

# Progression of Learning in Elementary School

## Mathematics

### Arithmetic

Understanding and writing numbers						
→ Student constructs knowledge with teacher guidance. ★ Student applies knowledge by the end of the school year. Student reinvests knowledge.	Elementary					
	Cycle One		Cycle Two		Cycle Three	
	1	2	3	4	5	6
<b>A. Natural numbers less than . . .</b>	<b>1000</b>		<b>100 000</b>		<b>1 000 000</b>	
1. Counts or recites counting rhymes involving natural numbers						
a. counts forward from a given number	→	★				
b. counts forward or backward	→	★	→	★	→	★
c. skip counts (e.g. by twos)	→	★	→	★	→	★
2. Counts collections (using objects or drawings)						
a. matches the gesture to the corresponding number word; recognizes the cardinal aspect of a number and the conservation of number in various combinations		★				
b. counts from a given number	→	★				
c. counts a collection by grouping or regrouping	→	★	→	★	→	★
d. counts a pre-grouped collection			→	★	→	★
3. Reads and writes any natural number	→	★	→	★	→	★
4. Represents natural numbers in different ways or associates a number with a set of objects or drawings						
a. emphasis on apparent, accessible groupings using objects, drawings or unstructured materials (e.g. tokens, nesting cubes, groups of ten objects placed inside a bag and ten of these bags placed inside another container)	→	★				
b. emphasis on exchanging apparent, non-accessible groupings, using structured		→	→	★		

<p>materials (e.g. base ten blocks, number tables)</p> <p>Gizmos: <a href="#">Mascot Election (Pictographs and Bar Graphs)</a> <a href="#">Modeling Decimals (Base-10 Blocks)</a> <a href="#">Reaction Time 1 (Graphs and Statistics)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a></p>						
<p>c. emphasis on place value in non-apparent, non-accessible groupings, using materials for which groupings are symbolic (e.g. abacus, money)</p> <p>Gizmos: <a href="#">Cannonball Clowns (Number Line Estimation)</a> <a href="#">Modeling Decimals (Base-10 Blocks)</a></p>			→	→	→	★
<p>5. Composes and decomposes a natural number in a variety of ways (e.g. <math>123 = 100 + 23</math> <math>123 = 100 + 20 + 3</math> <math>123 = 50 + 50 + 20 + 3</math> <math>123 = 2 \times 50 + 30 - 7</math> <math>123 = 2 \times 60 + 3</math>)</p> <p>Gizmos: <a href="#">Number Line Frog Hop (Addition and Subtraction)</a></p>	→	★	→	★	→	★
<p>6. Identifies equivalent expressions (e.g. <math>52 = 40 + 12</math>, <math>25 + 27 = 40 + 12</math>, <math>52 = 104 \div 2</math>)</p>	→	★	→	★	→	★
<p>7. Compares natural numbers</p>	→	★	→	★	→	★
<p>8. Arranges natural numbers in increasing or decreasing order</p>	→	★	→	★	→	★
<p>9. Describes number patterns, using his/her own words and appropriate mathematical vocabulary (e.g. even numbers, odd numbers, square numbers, triangular numbers, prime numbers, composite numbers)</p> <p>Gizmos: <a href="#">Factor Trees (Factoring Numbers)</a> <a href="#">Pattern Flip (Patterns)</a></p>	→	★	→	★	→	★

10. Locates natural numbers using different visual aids (e.g. hundreds chart, number strip, number line) Gizmos: <a href="#">Cannonball Clowns (Number Line Estimation)</a> <a href="#">Fraction Garden (Comparing Fractions)</a> <a href="#">Modeling Fractions (Area Models)</a>	→	★	→	★	→	★
11. Identifies properties of natural numbers						
a. odd or even numbers	→	★				
b. square, prime or composite numbers Gizmos: <a href="#">Factor Trees (Factoring Numbers)</a>			→	★		
12. Classifies natural numbers in various ways, based on their properties (e.g. even numbers, composite numbers)	→	★	→	★	→	★
13. Approximates a collection, using objects or drawings (e.g. estimate, round up/down to a given value) Gizmo: <a href="#">Measuring Motion</a>	→	★	→	★	→	★
14. Represents the power of a natural number				→		★
<b>Vocabulary</b> Grouping, digit, number, unit, tens place, hundreds place Natural number, even number, odd number <i>Is equal to, is bigger than (is greater than); is smaller than (is less than)</i> Increasing order, decreasing order Number line <b>Symbols</b> 0 to 9, <, >, =, numbers written using digits	→	★				
<b>Vocabulary</b> Base ten, position, place value, thousand, thousands place, ten thousands <i>Is not equal to; is greater than; is less than</i> Square number, composite number, prime number <b>Symbols</b> ≠, numbers written using digits			→	★		
<b>Vocabulary</b> Hundred thousands, million					→	★

Exponent, power, squared, cubed Parenthesis <b>Symbols</b> ( ), numbers written using digits, exponential notation						
<b>B. Fractions (using objects or drawings)</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Identifies fractions related to everyday items (using objects or drawings)	→	★				
2. Represents a fraction in a variety of ways, based on a whole or a collection of objects Gizmos: <a href="#">Equivalent Fractions (Fraction Tiles)</a> <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction Garden (Comparing Fractions)</a> <a href="#">Modeling Fractions (Area Models)</a> <a href="#">Toy Factory (Set Models of Fractions)</a>	→	→	→	→	→	★
3. Matches a fraction to part of a whole (congruent or equivalent parts) or part of a group of objects, and vice versa Gizmos: <a href="#">Adding Fractions (Fraction Tiles)</a> <a href="#">Equivalent Fractions (Fraction Tiles)</a> <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction Garden (Comparing Fractions)</a> <a href="#">Fractions Greater than One (Fraction Tiles)</a> <a href="#">Modeling Fractions (Area Models)</a>			→	★		
4. Identifies the different meanings of fractions (sharing, division, ratio)			→	→	→	→
5. Distinguishes a numerator from a denominator			→	★		
6. Reads and writes a fraction Gizmos: <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a>			→	★		
7. Compares a fraction to 0, $\frac{1}{2}$ or 1 Gizmos:			→	★		

<a href="#">Equivalent Fractions (Fraction Tiles)</a> <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction Garden (Comparing Fractions)</a> <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Fractions (Area Models)</a>						
<p>8. Verifies whether two fractions are equivalent</p> <p>Gizmos:</p> <a href="#">Adding Fractions (Fraction Tiles)</a> <a href="#">Equivalent Fractions (Fraction Tiles)</a> <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction Garden (Comparing Fractions)</a> <a href="#">Fractions Greater than One (Fraction Tiles)</a> <a href="#">Modeling Fractions (Area Models)</a>			→	→	→	★
<p>9. Matches a decimal or percentage to a fraction</p> <p>Gizmo:</p> <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Treasure Hunter (Decimals on the Number Line)</a>				→	→	★
<p>10. Orders fractions with the same denominator</p> <p>Gizmo:</p> <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction Garden (Comparing Fractions)</a> <a href="#">Modeling Fractions (Area Models)</a>				→	★	
<p>11. Orders fractions where one denominator is a multiple of the other(s)</p> <p>Gizmo:</p> <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction Garden (Comparing Fractions)</a> <a href="#">Modeling Fractions (Area Models)</a>					→	★

<p>12. Orders fractions with the same numerator</p> <p>Gizmo:</p> <p><a href="#">Fraction Artist 1 (Area Models of Fractions)</a></p> <p><a href="#">Fraction Artist 2 (Area Models of Fractions)</a></p> <p><a href="#">Fraction Garden (Comparing Fractions)</a></p> <p><a href="#">Modeling Fractions (Area Models)</a></p>					→	★
<p>13. Locates fractions on a number line</p> <p>Gizmo:</p> <p><a href="#">Fraction Artist 1 (Area Models of Fractions)</a></p> <p><a href="#">Fraction Artist 2 (Area Models of Fractions)</a></p> <p><a href="#">Fraction Garden (Comparing Fractions)</a></p> <p><a href="#">Modeling Fractions (Area Models)</a></p>					→	★
<p><b>Vocabulary</b> Fraction, half, one third, one quarter</p>	→	★				
<p><b>Vocabulary</b> Numerator, denominator Whole, equivalent part, equivalent fraction</p> <p><b>Symbol</b> Fractional notation</p>			→	★		
<p><b>c. Decimals up to . . .</b></p>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
				hundredths	thousandths	
<p>1. Represents decimals in a variety of ways (using objects or drawings)</p> <p>Gizmos:</p> <p><a href="#">Adding Decimals (Base-10 Blocks)</a></p> <p><a href="#">Factor Trees (Factoring Numbers)</a></p> <p><a href="#">Fraction Artist 1 (Area Models of Fractions)</a></p> <p><a href="#">Fraction Artist 2 (Area Models of Fractions)</a></p> <p><a href="#">Modeling Decimals (Area and Grid Models)</a></p> <p><a href="#">Modeling Decimals (Base-10 Blocks)</a></p> <p><a href="#">Subtracting Decimals (Base-10 Blocks)</a></p> <p><a href="#">Toy Factory (Set Models of Fractions)</a></p>			→	★	→	★
<p>2. Identifies equivalent representations (using objects or drawings)</p> <p>Gizmos:</p> <p><a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a></p> <p><a href="#">Modeling Decimals (Area and Grid Models)</a></p>			→	★	→	★
<p>3. Reads and writes numbers written in decimal notation</p>			→	★	→	★

Gizmos: <a href="#">Modeling Decimals (Base-10 Blocks)</a> <a href="#">Treasure Hunter (Decimals on the Number Line)</a>						
4. Understands the role of the decimal point Gizmos: <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Decimals (Area and Grid Models)</a>			→	★		
5. Composes and decomposes a decimal written in decimal notation Gizmos <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Decimals (Area and Grid Models)</a> <a href="#">Number Line Frog Hop (Addition and Subtraction)</a>			→	★	→	★
6. Recognizes equivalent expressions (e.g. 12 tenths is equivalent to 1 unit and 2 tenths; 0.5 is equivalent to 0.50) Gizmos: <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Decimals (Area and Grid Models)</a>			→	★	→	★
7. Locates decimals on a number line						
a) between two consecutive natural numbers Gizmos: <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a>			→	★	→	★
b) between two decimals Gizmo: <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Decimals (Area and Grid Models)</a> <a href="#">Modeling Decimals (Base-10 Blocks)</a> <a href="#">Treasure Hunter (Decimals on the Number Line)</a>				→	→	★
8. Compares two decimals Gizmos: <a href="#">Adding Decimals (Base-10 Blocks)</a> <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Decimals (Area and Grid Models)</a>			→	★	→	★

<a href="#">Modeling Decimals (Base-10 Blocks)</a> <a href="#">Treasure Hunter (Decimals on the Number Line)</a>						
9. Approximates (e.g. estimates, rounds to a given value, truncates decimal places) Gizmos: <a href="#">Rounding Whole Numbers (Number Line)</a> <a href="#">Target Sum Card Game (Multi-digit Addition)</a>			→	★	→	★
10. Arranges decimals in increasing or decreasing order Gizmos: <a href="#">Adding Decimals (Base-10 Blocks)</a> <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Decimals (Area and Grid Models)</a> <a href="#">Modeling Decimals (Base-10 Blocks)</a> <a href="#">Treasure Hunter (Decimals on the Number Line)</a>			→	★	→	★
11. Matches						
a. a fraction to its decimal Gizmos: <a href="#">Fraction Artist 1 (Area Models of Fractions)</a> <a href="#">Fraction Artist 2 (Area Models of Fractions)</a> <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Modeling Decimals (Area and Grid Models)</a> <a href="#">Treasure Hunter (Decimals on the Number Line)</a>			→	★		
b. a fraction or percentage to its decimal Gizmos: <a href="#">Fraction, Decimal, Percent (Area and Grid Models)</a> <a href="#">Treasure Hunter (Decimals on the Number Line)</a>					→	★
<b>Vocabulary</b> Decimal, tenth, hundredth <b>Symbol</b> Decimal notation			→	★		
<b>Vocabulary</b> Thousandth <b>Symbol</b> Decimal notation					→	★
<b>D. Integers</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>

1. Represents integers in a variety of ways (using objects or drawings) (e.g. tokens in two different colours, number line, thermometer, football field, elevator, hot air balloon)				→	→	★
2. Reads and writes integers					→	★
3. Locates integers on a number line or Cartesian plane Gizmos: <a href="#">City Tour (Coordinates)</a> <a href="#">Comparing and Ordering Integers</a>					→	★
4. Compares integers Gizmos: <a href="#">Comparing and Ordering Integers</a>					→	★
5. Arranges integers in increasing or decreasing order Gizmos: <a href="#">Comparing and Ordering Integers</a>					→	★
<b>Vocabulary</b> Integer Negative number, positive number <b>Symbols</b> Integer notation, +/- calculator key					→	★

Meaning of operations involving numbers						
→ ★	Elementary					
	Cycle One		Cycle Two		Cycle Three	
	1	2	3	4	5	6
Student constructs knowledge with teacher guidance.						
Student applies knowledge by the end of the school year.						
Student reinvests knowledge.						
<b>A. Natural numbers less than . . .</b>	<b>1000</b>		<b>100 000</b>		<b>1 000 000</b>	
1. Determines the operation(s) to perform in a given situation	→	★	→	★	→	★
2. Uses objects, diagrams or equations to represent a situation and conversely, describes a situation represented by objects, diagrams or equations (use of different meanings of addition and subtraction)						

a. transformation (adding, taking away), uniting, comparing	→	★	→	★	→	★
b. composition of transformations: positive, negative			→	★	→	★
c. composition of mixed transformations						
Gizmos: <a href="#">Quilting Bee (Symmetry)</a> <a href="#">Rock Art (Transformations)</a>						
3. Uses objects, diagrams or equations to represent a situation and conversely, describes a situation represented by objects, diagrams or equations (use of different meanings of multiplication and division)						
a. rectangular arrays, repeated addition, Cartesian product, sharing, and number of times $x$ goes into $y$ (using objects and diagrams)	→	★				
b. rectangular arrays, repeated addition, Cartesian product, area, volume, repeated subtraction, sharing, number of times $x$ goes into $y$ , and comparisons (using objects, diagrams or equations)			→	★	→	★
Gizmos: <a href="#">Chocomatic (Multiplication, Arrays, and Area)</a> <a href="#">Critter Count (Modeling Multiplication)</a> <a href="#">No Alien Left Behind (Division with Remainders)</a>						
4. Establishes equality relations between numerical expressions (e.g. $3 + 2 = 6 - 1$ )	→	★	→	★	→	★
5. Determines numerical equivalencies using relationships between						
a. operations (addition and subtraction) and the commutative property of addition	→	★				
b. operations (the four operations), the commutative property of addition and multiplication and the associative property			→	★		
Gizmos:						

<a href="#">Critter Count (Modeling Multiplication)</a> <a href="#">Function Machines 3 (Functions and Problem Solving)</a> <a href="#">Number Line Frog Hop (Addition and Subtraction)</a>						
<p>c. operations (the four operations), the commutative property of addition and multiplication, the associative property and the distributive property of multiplication over addition or subtraction</p> <p>Gizmos:  <a href="#">Chocomatic (Multiplication, Arrays, and Area)</a>  <a href="#">Critter Count (Modeling Multiplication)</a></p>					→	★
6. Translates a situation using a series of operations in accordance with the order of operations					→	★
<b>Vocabulary</b> Plus, minus, less, more Addition, subtraction, sum, difference <b>Symbols</b> +, -	→	★				
<b>Vocabulary</b> At least, at most, term, missing term Multiplication, factor, product Division, divisor, dividend, quotient, remainder, sharing Equality, inequality, equation, inverse operation, multiple <b>Symbols</b> ×, ÷			→	★		
<b>B. Decimals up to . . .</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
			<b>hundredths</b>	<b>thousandths</b>		
1. Uses objects, diagrams or equations to represent a situation and conversely, describes a situation represented by objects, diagrams or equations (use of different meanings of addition and subtraction)						
a) transformation (adding, taking away), uniting, comparing			→	★	→	★
b) composition of transformations: positive, negative			→	★	→	★
c) composition of mixed transformations					→	★
Gizmos: <a href="#">Quilting Bee (Symmetry)</a>						

<a href="#">Rock Art (Transformations)</a>						
2. Uses objects, diagrams or equations to represent a situation and conversely, describes a situation represented by objects, diagrams or equations (use of different meanings of multiplication and division: rectangular arrays, Cartesian product, area, volume, sharing, number of times $x$ goes into $y$ , and comparisons)			→	★	→	★
3. Determines numerical equivalencies using						
a. the relationship between operations (addition and subtraction), the commutative property of addition and the associative property  Gizmos: <a href="#">Adding Decimals (Base-10 Blocks)</a> <a href="#">Function Machines 3 (Functions and Problem Solving)</a> <a href="#">Number Line Frog Hop (Addition and Subtraction)</a> <a href="#">Subtracting Decimals (Base-10 Blocks)</a>			→	★		
b. relationships between operations (the four operations), the commutative property of addition and multiplication, the associative property and the distributive property of multiplication over addition or subtraction  Gizmos: <a href="#">Chocomatic (Multiplication, Arrays, and Area)</a> <a href="#">Critter Count (Modeling Multiplication)</a>					→	★
4. Translates a situation into a series of operations in accordance with the order of operations					→	★
<b>C. Fractions</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Uses objects, diagrams or equations to represent a situation and conversely, describes a situation represented by objects, diagrams or equations (use of different meanings of addition, subtraction and multiplication by a natural number)					→	★

Operations involving numbers						
→ Student constructs knowledge with teacher guidance. ★ Student applies knowledge by the end of the school year. Student reinvests knowledge.	Elementary					
	Cycle One		Cycle Two		Cycle Three	
A. Natural numbers (based on the benchmarks for each cycle)	1	2	3	4	5	6
1. Approximates the result of						
a. an addition or subtraction involving natural numbers	→	★				
b. any of the four operations involving natural numbers						
Gizmos: <a href="#">Chocomatic (Multiplication, Arrays, and Area)</a> <a href="#">Multiplying Decimals (Area Model)</a>			→	→	→	★
2. Builds a repertoire of memorized addition and subtraction facts <sup>1</sup>						
a. Builds a memory of addition facts <sup>2</sup> (0 + 0 to 10 + 10) and the corresponding subtraction facts, using objects, drawings, charts or tables	→	★				
b. Develops various strategies that promote mastery of number facts and relates them to the properties of addition	→	→	★			
c. Masters all addition facts (0 + 0 to 10 + 10) and the corresponding subtraction facts	→	→	★			
3. Develops processes for mental computation						

<p>a. Uses his/her own processes to determine the sum or difference of two natural numbers</p>	→	★				
<p>b. Uses his/her own processes to determine the product or quotient of two natural numbers</p> <p>Gizmos: <a href="#">Multiplying Decimals (Area Model)</a></p>			→	→	→	★
<p>4. Develops processes for written computation (addition and subtraction)</p>						
<p>a. Uses his/her own processes as well as objects and drawings to determine the sum or difference of two natural numbers less than 1000</p>	→	★				
<p>b. Uses conventional processes to determine the sum of two natural numbers of up to four digits</p>			→	★		
<p>c. Uses conventional processes to determine the difference between two natural numbers of up to four digits whose result is greater than 0</p>			→	★		
<p>5. Determines the missing term in an equation (relationships between operations): <math>a + b = \square</math>, <math>a + \square = c</math>, <math>\square + b = c</math>, <math>a - b = \square</math>, <math>a - \square = c</math>, <math>\square - b = c</math></p> <p>Gizmos: <a href="#">Function Machines 3 (Functions and Problem Solving)</a> <a href="#">Number Line Frog Hop (Addition and Subtraction)</a></p>	→	★				
<p>6. Builds a repertoire of memorized multiplication and division facts</p>						
<p>a. Builds a memory of multiplication facts (<math>0 \times 0</math> to <math>10 \times 10</math>) and the corresponding division facts, using objects, drawings, charts or tables</p> <p>Gizmos: <a href="#">Factor Trees (Factoring Numbers)</a></p>			→	★		
<p>b. Develops various strategies that promote mastery of number facts and relate them to the properties of multiplication</p> <p>Gizmos: <a href="#">Factor Trees (Factoring Numbers)</a> <a href="#">Multiplying Decimals (Area Model)</a></p>			→	→	★	

<p>c. Masters all multiplication facts (<math>0 \times 0</math> to <math>10 \times 10</math>) and the corresponding division facts</p> <p>Gizmos: <a href="#">Factor Trees (Factoring Numbers)</a></p>			→	→	★	
7. Develops processes for written computation (multiplication and division)						
<p>a. Uses his/her own processes as well as materials and drawings to determine the product or quotient of a three-digit natural number and a one-digit natural number, expresses the remainder of a division as a fraction, depending on the context</p> <p>Gizmos: <a href="#">Multiplying Decimals (Area Model)</a></p>			→	★		
<p>b. Uses conventional processes to determine the product of a three-digit natural number and a two-digit natural number</p>				→	★	
<p>c. Uses conventional processes to determine the quotient of a four-digit natural number and a two-digit natural number, expresses the remainder of a division as a decimal that does not go beyond the second decimal place</p>				→	★	
<p>8. Determines the missing term in an equation (relationships between operations): <math>a \times b = \square</math>, <math>a \times \square = c</math>, <math>\square \times b = c</math>, <math>a \div b = \square</math>, <math>a \div \square = c</math>, <math>\square \div b = c</math></p> <p>Gizmos: <a href="#">Function Machines 3 (Functions and Problem Solving)</a></p>			→	→	→	★
<p>9. Decomposes a number into prime factors</p> <p>Gizmos: <a href="#">Factor Trees (Factoring Numbers)</a> <a href="#">Number Line Frog Hop (Addition and Subtraction)</a></p>				→	→	★
<p>10. Calculates the power of a number</p>				→	★	
<p>11. Determines the divisibility of a number by 2, 3, 4, 5, 6, 8, 9, 10</p>				→	★	
<p>12. Performs a series of operations in accordance with the order of operations</p>				→	★	

13. Using his/her own words and mathematical language that is at an appropriate level for the cycle, describes						
<p>a. non-numerical patterns (e.g. series of colours, shapes, sounds, gestures)</p> <p>Gizmos: <a href="#">Pattern Flip (Patterns)</a></p>	→	★				
<p>b. numerical patterns (e.g. number rhymes, tables and charts)</p> <p>Gizmos: <a href="#">Mascot Election (Pictographs and Bar Graphs)</a> <a href="#">Pattern Flip (Patterns)</a> <a href="#">Reaction Time 1 (Graphs and Statistics)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a></p>	→	★				
c. series of numbers and family of operations	→	→	→	→	→	★
<p>14. Adds new terms to a series when the first three terms or more are given</p> <p>Gizmos: <a href="#">Pattern Flip (Patterns)</a></p>	→	→	→	→	→	★
15. Uses a calculator and						
a. becomes familiar with its basic functions (+, -, =, 0 to 9 number keys, all clear, clear)	→	★				
<p>b. becomes familiar with its × and ÷ functions</p> <p>Gizmos: <a href="#">No Alien Left Behind (Division with Remainders)</a></p>			→	★		
c. becomes familiar with memory keys and change of sign keys (+/-)					→	★
<p><b>Vocabulary</b> Pattern, series <b>Symbols</b> Calculator keys</p>	→	★				
<b>B. Fractions (using objects or diagrams)</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>

<p>1. Generates a set of equivalent fractions</p> <p>Gizmos:</p> <p><a href="#">Equivalent Fractions (Fraction Tiles)</a></p> <p><a href="#">Fraction Artist 1 (Area Models of Fractions)</a></p> <p><a href="#">Fraction Artist 2 (Area Models of Fractions)</a></p> <p><a href="#">Fraction Garden (Comparing Fractions)</a></p> <p><a href="#">Toy Factory (Set Models of Fractions)</a></p>				→	→	→ ★
<p>2. Reduces a fraction to its simplest form (lowest terms)</p> <p>Gizmos:</p> <p><a href="#">Equivalent Fractions (Fraction Tiles)</a></p>					→	★
<p>3. Adds and subtracts fractions when the denominator of one fraction is a multiple of the other fraction(s)</p> <p>Gizmos;</p> <p><a href="#">Adding Fractions (Fraction Tiles)</a></p>					→	★
<p>4. Multiplies a natural number by a fraction</p>					→	★
<p><b>Vocabulary</b></p> <p>Irreducible fraction</p>					→	★
<p><b>C. Decimals</b></p>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
<p>1. Approximates the result of</p>						
<p>a. an addition or a subtraction</p> <p>Gizmos:</p> <p><a href="#">Adding Decimals (Base-10 Blocks)</a></p> <p><a href="#">Subtracting Decimals (Base-10 Blocks)</a></p> <p><a href="#">Treasure Hunter (Decimals on the Number Line)</a></p>				→	→	→ ★
<p>b. a multiplication or division</p> <p>Gizmos:</p> <p><a href="#">Multiplying Decimals (Area Model)</a></p>					→	★
<p>2. Develops processes for mental computation</p>						



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## Geometry

→ Student constructs knowledge with teacher guidance. ★ Student applies knowledge by the end of the school year. Student reinvests knowledge.	Elementary					
	Cycle One		Cycle Two		Cycle Three	
A. Space	1	2	3	4	5	6
1. Gets his/her bearings and locates objects in space (spatial relationships)	→	★				
2. Locates objects in a plane	→	→	→	★		
3. Locates objects on an axis (based on the types of numbers studied)	→	★	→	★	→	★
4. Locates points in a Cartesian plane						
a) in the first quadrant	→	→	→	★		
b) in all four quadrants						
Gizmos: <a href="#">City Tour (Coordinates)</a>					→	★
<b>Vocabulary</b> Reference system, plane, Cartesian plane, ordered pair	→	→	→	★		
<b>Symbols</b> Writing ordered pairs ( $a, b$ )	→	→	→	→	→	★
B. Solids	1	2	3	4	5	6
1. Compares objects or parts of objects in the environment with solids (e.g. spheres, cones, cubes, cylinders, prisms, pyramids)	→	★				
2. Compares and constructs solids (e.g. spheres, cones, cubes, cylinders, prisms, pyramids)	→	★				
3. Identifies the main solids (e.g. spheres, cones, cubes, cylinders, prisms, pyramids)	→	★				
<b>Vocabulary</b> Solid, base of a solid, face, flat surface, curved surface Sphere, cone, cube, cylinder, prism, pyramid	→	★				
4. Identifies and represents the different faces of a prism or pyramid	→	★				

5. Describes prisms and pyramids in terms of faces, vertices and edges			→	★		
6. Classifies prisms and pyramids			→	★		
7. Constructs a net of a prism or pyramid			→	★		
8. Matches the net of						
a. a prism to the corresponding prism and vice versa		→	→	★		
b. a pyramid to the corresponding pyramid and vice versa		→	→	★		
c. a convex polyhedron to the corresponding convex polyhedron					→	★
<b>Vocabulary</b> Vertex, edge, net of a solid			→	★		
9. Tests Euler's theorem on convex polyhedrons					→	★
<b>Vocabulary</b> Polyhedron, convex polyhedron					→	★
<b>c. Plane figures</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Compares and constructs figures made with closed curved lines or closed straight lines	→	★				
2. Identifies plane figures (square, rectangle, triangle, rhombus and circle)	→	★				
3. Describes plane figures (square, rectangle, triangle and rhombus)	→	★				
<b>Vocabulary</b> Straight line, closed straight line, curved line Plane figure, side Square, circle, rectangle, triangle, rhombus	→	★				
4. Describes convex and nonconvex polygons			→	★		
5. Identifies and constructs parallel lines and perpendicular lines			→	★		
6. Describes quadrilaterals (e.g. parallel segments, perpendicular segments, right angles, acute angles, obtuse angles)			→	★		
7. Classifies quadrilaterals			→	★		
<b>Vocabulary</b> Quadrilateral, parallelogram, trapezoid, polygon Convex polygon, nonconvex polygon, segment <i>Is parallel to . . . ; is perpendicular to . . .</i> <b>Symbols</b>			→	★		

//, $\perp$						
8. Describes triangles: scalene triangles, right triangles, isosceles triangles, equilateral triangles					→	★
9. Classifies triangles					→	★
10. Describes circles					→	★
<b>Vocabulary</b> Equilateral triangles, isosceles triangle, right triangle, scalene triangle Circle, central angle, diameter, radius, circumference					→	★
<b>D. Frieze patterns and tessellations</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Identifies congruent figures	→	★				
2. Observes and produces patterns using geometric figures	→	→	→	★		
3. Observes and produces frieze patterns and tessellations						
a. using reflections						
Gizmos: <a href="#">Pattern Flip (Patterns)</a> <a href="#">Quilting Bee (Symmetry)</a> <a href="#">Rock Art (Transformations)</a>				→	★	
b. using translations						
Gizmos: <a href="#">Pattern Flip (Patterns)</a> <a href="#">Rock Art (Transformations)</a>					→	★
<b>Vocabulary</b> Frieze pattern, tessellation Reflection, line of reflection, symmetric figure				→	★	
<b>Vocabulary</b> Translation, translation arrow					→	★

# Measurement

→ Student constructs knowledge with teacher guidance. ★ Student applies knowledge by the end of the school year. Student reinvests knowledge.	Elementary					
	Cycle One		Cycle Two		Cycle Three	
A. Lengths	1	2	3	4	5	6
1. Compares lengths	→	★				
2. Constructs rulers	→	★				
3. Estimates and measures the dimensions of an object using unconventional units	→	★				
4. Estimates and measures the dimensions of an object using conventional units						
a. metre, decimetre and centimetre	→	★				
b. metre, decimetre, centimetre and millimeter						
Gizmos: <a href="#">Measuring Motion</a> <a href="#">Measuring Trees</a>			→	★		
c. metre, decimetre, centimetre, millimetre and kilometer						
Gizmos: <a href="#">Measuring Motion</a> <a href="#">Measuring Trees</a>					→	★
5. Establishes relationships between units of measure for length						
a. metre, decimetre, centimetre and millimeter						
Gizmos: <a href="#">Measuring Trees</a>			→	★		
b. metre, decimetre, centimetre, millimetre and kilometer					→	★
Gizmos:						

<a href="#">Measuring Trees</a>						
6. Calculates the perimeter of plane figures			→	★		
<b>Vocabulary</b> Width, length, height, depth Unit of measure, centimetre, decimetre, metre <b>Symbols</b> m, dm, cm		→	★			
<b>Vocabulary</b> Perimeter, millimetre <b>Symbol</b> mm			→	★		
<b>Vocabulary</b> Kilometre <b>Symbol</b> km				→	★	
<b>B. Surface areas</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Estimates and measures surface area						
a) using unconventional units Gizmos: <a href="#">Measuring Motion</a>			→	★		
b) using conventional units Gizmo: <a href="#">Measuring Motion</a>					→	★
<b>Vocabulary</b> Surface, area			→	★		
<b>Vocabulary</b> Square centimetre, square decimetre, square metre <b>Symbols</b> $m^2$ , $dm^2$ , $cm^2$					→	★
<b>C. Volumes</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Estimates and measures volume						
a. using unconventional units Gizmo:			→	★		

<a href="#">Balancing Blocks (Volume)</a>						
b. using conventional units						
Gizmo: <a href="#">Balancing Blocks (Volume)</a>					→	★
<b>Vocabulary</b> Volume			→	★		
<b>Vocabulary</b> Cubic centimetre, cubic decimetre, cubic metre <b>Symbols</b> $m^3$ , $dm^3$ , $cm^3$					→	★
<b>D. Angles</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Compares angles			→	★		
<b>Vocabulary</b> Angle, right angle, acute angle, obtuse angle			→	★		
2. Estimates and determines the degree measurement of angles					→	★
Gizmo: <a href="#">Measuring Motion</a>						
<b>Vocabulary</b> Degree, protractor <b>Symbols</b> $\sphericalangle$ , $^\circ$					→	★
<b>E. Capacities</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Estimates and measures capacity using unconventional units			→	→	★	
2. Estimates and measures capacity using conventional units			→	→	★	
3. Establishes relationships between units of measure (e.g. : 1 L = 1000 mL, $\frac{1}{2}$ L = 500 mL)					★	
<b>Vocabulary</b> Capacity, litre, millilitre <b>Symbols</b> L, mL				→	★	
<b>F. Masses</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>

1. Estimates and measures mass using unconventional units Gizmo: <a href="#">Measuring Motion</a> <a href="#">Measuring Trees</a>			→	→	→	★
2. Estimates and measures mass using conventional units Gizmo: <a href="#">Measuring Motion</a> <a href="#">Measuring Trees</a>			→	→	→	★
3. Establishes relationships between units of measure (e.g. : 1 kg = 1000 g, $\frac{1}{2}$ kg = 500 g)					→	★
<b>Vocabulary</b> Mass, gram, kilogram <b>Symbols</b> g, kg					→	★
<b>G. Time</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Estimates and measures time using conventional units Gizmo: <a href="#">Measuring Motion</a> <a href="#">Measuring Trees</a>	→	→	→	★		
2. Establishes relationships between units of measure	→	→	→	→	→	★
<b>Vocabulary</b> Day, hour, minute, second <b>Symbols</b> h, min, s, representation of time: 3 h, 3 h 25 min, 03:25, 3:25 a.m.	→	★				
<b>Vocabulary</b> Daily cycle, weekly cycle, yearly cycle	→	→	→	★		
<b>H. Temperatures</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
1. Estimates and measures temperature using conventional units	→	→	→	→	→	★
<b>Vocabulary</b> Degree Celsius <b>Symbol</b>	→	★				

## Statistics

→ ★ Student constructs knowledge with teacher guidance. Student applies knowledge by the end of the school year. Student reinvests knowledge.	Elementary					
	Cycle One		Cycle Two		Cycle Three	
	1	2	3	4	5	6
1. Formulates questions for a survey (based on age-appropriate topics, students' language level, etc.) Gizmo: <a href="#">Mascot Election (Pictographs and Bar Graphs)</a>	→	→	→	→	→	★
2. Collects, describes and organizes data (classifies or categorizes) using tables Gizmos: <a href="#">Mascot Election (Pictographs and Bar Graphs)</a> <a href="#">Movie Reviewer (Mean and Median)</a> <a href="#">Reaction Time 1 (Graphs and Statistics)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a>	→	→	→	→	→	★
3. Interprets data using						
a. a table, a bar graph and a pictograph Gizmos: <a href="#">Elevator Operator (Line Graphs)</a> <a href="#">Graphing Skills</a> <a href="#">Mascot Election (Pictographs and Bar Graphs)</a> <a href="#">Reaction Time 1 (Graphs and Statistics)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a>	→	★				
b. a table, a bar graph, a pictograph and a broken-line graph			→	★		
c. a table, a bar graph, a pictograph, a broken-line graph and a circle graph Gizmos: <a href="#">Elevator Operator (Line Graphs)</a> <a href="#">Graphing Skills</a>					→	★

<a href="#">Mascot Election (Pictographs and Bar Graphs)</a> <a href="#">Reaction Time 1 (Graphs and Statistics)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a>							
4. Displays data using							
a. a table, a bar graph and a pictograph  Gizmos: <a href="#">Elevator Operator (Line Graphs)</a> <a href="#">Graphing Skills</a> <a href="#">Mascot Election (Pictographs and Bar Graphs)</a> <a href="#">Reaction Time 1 (Graphs and Statistics)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a>						→ ★	
b. a table, a bar graph, a pictograph and a broken-line graph  Gizmos: <a href="#">Elevator Operator (Line Graphs)</a> <a href="#">Graphing Skills</a> <a href="#">Mascot Election (Pictographs and Bar Graphs)</a> <a href="#">Reaction Time 1 (Graphs and Statistics)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a>						→ ★	
5. Understands and calculates the arithmetic mean							
Gizmos: <a href="#">Movie Reviewer (Mean and Median)</a> <a href="#">Reaction Time 2 (Graphs and Statistics)</a>						→ ★	
<b>Vocabulaire</b> Survey, table Bar graph, pictograph		★					
<b>Vocabulaire</b> Broken-line graph				→ ★			
<b>Vocabulaire</b> Circle graph, arithmetic mean						→ ★	

# Probability

→ Student constructs knowledge with teacher guidance. ★ Student applies knowledge by the end of the school year. Student reinvests knowledge.	Elementary					
	Cycle One		Cycle Two		Cycle Three	
	1	2	3	4	5	6
1. When applicable, recognizes variability in possible outcomes (uncertainty)	→	→	→	→	→	★
2. When applicable, recognizes equiprobability (e.g. quantity, symmetry of an object [cube]) Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>	→	→	→	→	→	★
3. When applicable, becomes aware of the independence of events in an experiment Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>	→	→	→	→	→	★
4. Experiments with activities involving chance, using various objects (e.g. spinners, rectangular prisms, glasses, marbles, thumb tacks, 6-, 8- or 12-sided dice) Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>	→	→	→	→	→	★
5. Predicts qualitatively an outcome or several events using a probability line, among other things						
a. certain, possible or impossible outcome Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>	→	→	→	→	→	★
b. more likely, just as likely, less likely event Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>			→	→	→	★

6. Distinguishes between prediction and outcome Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>	→	→	→	→	→	★
7. Uses tables or diagrams to collect and display the outcomes of an experiment Gizmo: <a href="#">Mascot Election (Pictographs and Bar Graphs)</a>	→	→	→	→	→	★
8. Enumerates possible outcomes of						
a. a simple random experiment	→	★				
b. a random experiment, using a table, a tree diagram Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>			→	→	→	★
9. Compares qualitatively the theoretical or experimental probability of events Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>			→	→	→	★
10. Recognizes that a probability is always between 0 and 1 Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>				→		★
11. Uses fractions, decimals or percentages to quantify a probability				→		★
12. Compares the outcomes of a random experiment with known theoretical probabilities Gizmos: <a href="#">Spin the Big Wheel! (Probability)</a>				→		★
13. Simulates random experiments with or without the use of technology Gizmos:			→	→	→	★

<a href="#">Spin the Big Wheel! (Probability)</a>						
<b>Vocabulary</b> Chance, random experiment, enumeration, tree diagram Certain outcome, possible outcome, impossible outcome Event, likely, just as likely, more likely, less likely, event probability	→	→	→	★		